
<Your Faculty>
<YOUR THESIS TITLE>
<Your Thesis Title>

Doctor of Philosophy
(Computer Science)
2015

## ACKNOWLEDGEMENTS

Thanks to all who have helped.


#### Abstract

This is the English abstract. Auto single-line spacing. Jelly dessert sesame snaps. Oat cake jelly oat cake gingerbread sweet roll apple pie muffin sesame snaps. Dragée icing carrot cake faworki tart chocolate cake. Cookie apple pie chupa chups tootsie roll sweet roll toffee chocolate bar gummies gummi bears. Apple pie lollipop candy canes jujubes caramels. Soufflé powder liquorice fruitcake. Tiramisu fruitcake candy canes jelly beans muffin chupa chups bonbon. Donut sugar plum fruitcake liquorice chocolate pastry lollipop chocolate bar cookie. Jellyo donut marshmallow chupa chups danish. Sugar plum pudding sweet roll muffin applicake biscuit tart fruitcake wafer. Pudding croissant carrot cake tiramisu candy canes. Powder powder jelly-o. Pie croissant cake chocolate cake carrot cake sweet apple pie sweet roll donut.


# <TERJEMAHAN TAJUK TESIS DALAM BAHASA <br> MELAYU> 

## ABSTRAK

Inilah abstrak dalam Bahasa Melayu. Data korpus merupakan data bahasa Melayu yang datangnya dalam dua bentuk sumber, iaitu bentuk tulisan dan bentuk lisan. Bentuk tulisan seperti buku, majalah, surat khabar, makalah, monograf, dokumen, kertas kerja, efemeral, puisi, drama, kad bahan, surat, risalah dan sebagainya. Sementara bentuk lisan yang ditranskripsikan seperti ucapan, wawancara, temu bual, perbualan dan sebagainya dalam pelbagai bentuk rakaman.

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# LIST OF ABBREVIATIONS, SYMBOLS, SPECIALIZED NOMENCLATURE 

$b, c$ constants
$C_{f}$ local friction coefficient

## CHAPTER 1

## HOW TO USE THE UNIMASTHESIS DOCUMENT CLASS

UnimasThesis is a $\mathrm{IATEX}_{\mathrm{E}}$ class for authoring theses that fulfill formatting specifications required by Universiti Malaysia Sarawak (Unimas), Malaysia.

A sample thesis.tex is included in the package, which I recommend you modify for your own thesis write-up. You can rename the files, but I'll stick with the file name 'thesis.tex' throughout this guide.

### 1.1 Printing from Acrobat Reader

This is such an important point that I've decided to make it the first section:
In the Print... dialog, remember to

- set the paper size to $\mathbf{A 4}$;
- set page scaling to None or Actual size or $\mathbf{1 0 0 \%}$,
otherwise the page margins and visual font sizes would be incorrect!


### 1.2 Language Modes: English and Bahasa Malaysia

UnimasThesis uses the English language by default. If you are writing your thesis in Bahasa Malaysia, you should activate the bahasam mode like this:

```
\documentclass[bahasam]{UnimasThesis}
```


### 1.3 Author Information

You need to provide some author information in the preamble. Example lines from thesis. tex:

\title\{<Your Thesis Title>\}

\author $\{<$ Your Name>\}
\faculty\{<Your Faculty>\}

\facultyColour\{FFCCOO\} \%\% 6-digit RGB hexadecimal code
\submissionyear \{2015\}
\degreetype\{Doctor of Philosophy <br>(Technology and Innovation)\}

These information are needed to generate the preliminary pages.

### 1.4 Preliminary Pages

Once in the main document body, \frontmatter sets up the, well, front matter. This include setting the page numbers to lower-case Roman numerals. \maketitle will generate the cover page as well.
\begin\{document \} }
$\backslash$ frontmatter
\maketitle

The Malay and English abstracts, and the acknowledgements, are typeset with the enAbstract, msAbstract, acknowledgements environments:

## \begin\{enAbstract\} 

}This is the English abstract. ...
\end\{enAbstract\} }

```
\begin{msAbstract}[Terjemahan Tajuk Tesis]
Inilah abstrak dalam Bahasa Melayu. ...
\end{msAbstract}
\begin{acknowledgements}
This is the acknowledgements. ...
\end{acknowledgements}
```

Note that if your thesis is in English, you will need to provide the Bahasa Malaysia translation of your thesis title as an option to your msAbstract environment. The Bahasa Malaysia abstract will be automatically italicised.

Conversely, if your thesis is in Bahasa Malaysia (i.e. bahasam option is used), you will need to provide the English translation of your thesis title as an option to your enAbstract environment. The English abstract will be automatically italicised.

This is followed by the content lists:
\tableofcontents
\listoftables
\listoffigures

### 1.5 List of Abbreviations, Symbols, Specialized Nomenclature

These can be prepared using a tabular:
\chapter\{List of Abbreviations, Symbols, Specialized Nomenclature\}
\{

```
\begin{tabular}{1l}
$b, c$ & constants\\
$C_f$ & local friction coefficient\\
\end{tabular}
\par}
```


### 1.6 Main Chapters

Start the main text of your thesis with \mainmatter, followed by the usual chapters and sections:
\mainmatter
\chapter\{Introduction\}
...

\section\{...\}

You may want to use \include or \input to better organise your chapter files. Note however that a \include immediately after \mainmatter will cause problems in the TOC formatting. \input will have no problems.

### 1.7 Figures and Tables

Figures and tables can be inserted using the usual ways in ${ }^{\mathrm{LAT}} \mathrm{E}$. However, note that the Unimas formatting guidelines states
'It is advisable that all tables and figures are placed on separate pages and not together with the text.' (Graduate Studies Regulations, CGS UNIMAS 4th

Edition, p. 33)

To achieve this, use the [p!] placement option for your table and figure environments.

### 1.8 Bibliography

Specify your bibliography style and $\operatorname{BibT}_{\mathrm{E}} \mathrm{X}$ database file with

## \bibliography\{refs\}

The bibliography and citation style has been set to apacite, so you may want to consult the documentation of that package to get the most out of it.

### 1.9 Appendices

If you have any appendices, you can add them thus:
\appendix
\chapter\{Sample Code\}

You may want to use \include or \input to better organise your appendix files. Note however that a \include immediately after \appendix will cause problems in the appendix chapter headings. \input will have no problems.

## CHAPTER 2

## INTRODUCTION

### 2.1 What is Lorem Ipsum?

Lorem Ipsum is simply dummy text of the printing and typesetting industry. Lorem Ipsum has been the industry's standard dummy text ever since the 1500 s, when an unknown printer took a galley of type and scrambled it to make a type specimen book Banerjee and Pedersen (2003). It has survived not only five centuries, but also the leap into electronic typesetting, remaining essentially unchanged. It was popularised in the 1960s with the release of Letraset sheets containing Lorem Ipsum passages, and more recently with desktop publishing software like Aldus PageMaker including versions of Lorem Ipsum Berment (2004).

### 2.2 Where Does It Come From?

The pressure coefficient for an incompressible fluid is given by

$$
\begin{equation*}
C_{p}=\frac{P-P_{\infty}}{\frac{1}{2} \rho U_{\infty}^{2}}=1-\left(\frac{U_{1}}{U_{\infty}}\right)^{2}, \tag{2.1}
\end{equation*}
$$

where $P$ is the local static pressure, $P_{\infty}$ is the static pressure at the beginning of the inlet section ( $x=0 \mathrm{~m}$ ) and $U_{1}$ and $U_{\infty}$ are the local and inlet free stream velocities, respectively. Figure 1(b) shows the $C_{p}$ distribution for the APG and FPG cases. The test section is configured such that a $\operatorname{ZPG}\left(C_{p}=0 \pm 0.01\right)$ is maintained until $x \approx 3 \mathrm{~m}$, from which point a constant pressure gradient is maintained for both non-ZPG cases.

Contrary to popular belief, Lorem Ipsum is not simply random text. It has roots in a piece of classical Latin literature from 45 BC, making it over 2000 years old. Richard McClintock, a Latin professor at Hampden-Sydney College in Virginia, looked up one of the more obscure Latin words, consectetur, from a Lorem Ipsum passage, and going through the cites of the word in classical literature, discovered the undoubtable source Azarova, Mitrofanova, Sinopalnikova, Yavorskaya, and Oparin (2002); Budanitsky and Hirst (2006). Lorem Ipsum comes from sections 1.10.32 and 1.10.33 of "de Finibus Bonorum et Malorum" (The Extremes of Good and Evil) by Cicero, written in 45 BC . This book is a treatise on the theory of ethics, very popular during the Renaissance. The first line of Lorem Ipsum, ""'Lorem ipsum dolor sit amet. ..", comes from a line in section 1.10.32.

The standard chunk of Lorem Ipsum used since the 1500s is reproduced below for those interested. Sections 1.10.32 and 1.10.33 from "de Finibus Bonorum et Malorum" by Cicero are also reproduced in their exact original form, accompanied by English versions from the 1914 translation by H. Rackham.

$$
\begin{equation*}
-\frac{\left(x_{0}-\mu\right)^{2}}{2 \sigma^{2}}=-\ln 2 \tag{2.2}
\end{equation*}
$$

### 2.3 Examples

The first few paragraphs of Lorem Ipsum are given below.

### 2.3.1 First Paragraph

Lorem ipsum dolor sit amet, consectetur adipiscing elit. Donec posuere, neque quis feugiat egestas, quam sapien dictum justo, eu vulputate nunc metus sed dui. Integer molestie leo quis libero facilisis, dictum pretium quam ornare. Vestibulum ante ipsum primis in faucibus orci
luctus et ultrices posuere cubilia Curae; Vivamus luctus rutrum magna non convallis. Praesent vestibulum consequat eros, et fringilla nisi suscipit id. Nam vulputate justo dui, eu rutrum est accumsan ut. Sed molestie erat vitae mi blandit, in volutpat urna lobortis. Vestibulum mollis rutrum gravida. Fusce dolor nulla, condimentum vel pretium ut, venenatis eget leo. Ut semper placerat mauris, ut tempus est tempor vel. Interdum et malesuada fames ac ante ipsum primis in faucibus. In vitae feugiat diam. Pellentesque accumsan consequat turpis aliquam elementum.

### 2.3.2 Next Two Paragraphs

Vivamus dignissim arcu nunc, non aliquam sem porta vitae. Sed sodales accumsan dui sit amet egestas. Maecenas rhoncus a erat eget accumsan.

- Etiam vitae pulvinar metus, sed fringilla orci.
- Duis dapibus dolor risus, non ultrices enim porta sit amet.
- Ut eu libero augue.

Nulla ipsum augue, feugiat ac laoreet quis, pretium ut magna. Class aptent taciti sociosqu ad litora torquent per conubia nostra, per inceptos himenaeos. Integer blandit placerat dictum.

Sed dolor justo, scelerisque sed rutrum quis, porttitor a mauris. Cras non auctor felis, rutrum fringilla risus. Integer at convallis erat, sit amet luctus turpis. Duis sed rutrum eros, quis tempus risus. Etiam pellentesque nisi odio, eget dignissim eros ultrices et. Aliquam leo massa, fermentum vel odio sed, ullamcorper molestie lorem. Integer lorem felis, adipiscing sit amet interdum eget, auctor at lorem. Aliquam ultricies tortor eu nibh facilisis tincidunt.

## a. Some Notes

Duis sed rutrum eros, quis tempus risus. Etiam pellentesque nisi odio, eget dignissim eros ultrices et. Aliquam leo massa, fermentum vel odio sed, ullamcorper molestie lorem.

## b. And Further

Duis sed rutrum eros, quis tempus risus. Etiam pellentesque nisi odio, eget dignissim eros ultrices et. Aliquam leo massa, fermentum vel odio sed, ullamcorper molestie lorem.

### 2.3.3 Least-Squares with Forgetting Factor AdaptiveLaw

### 2.4 Mechatronic Suspension System; History and a Brief Background

Nulla ipsum augue, feugiat ac laoreet quis, pretium ut magna. Class aptent taciti sociosqu ad litora torquent per conubia nostra, per inceptos himenaeos. Integer blandit placerat dictum.

### 2.5 Summary

Nulla ipsum augue, feugiat ac laoreet quis, pretium ut magna. Class aptent taciti sociosqu ad litora torquent per conubia nostra, per inceptos himenaeos. Integer blandit placerat dictum.

Sed dolor justo, scelerisque sed rutrum quis, porttitor a mauris. Cras non auctor felis, rutrum fringilla risus. Integer at convallis erat, sit amet luctus turpis. Duis sed rutrum eros, quis tempus risus. Etiam pellentesque nisi odio, eget dignissim eros ultrices et. Aliquam leo massa, fermentum vel odio sed, ullamcorper molestie lorem. Integer lorem felis, adipiscing sit amet interdum eget, auctor at lorem. Aliquam ultricies tortor eu nibh facilisis tincidunt.

Table 2.1: Number of Jewels

| Type | Quantity |
| :--- | :---: |
| Sapphire | 6 |
| Diamond | 23 |
| Gold | 56 |
| Silver | 235 |
| Bronze | 324 |



Figure 2.1: Example figure

## CHAPTER 3

## FIBONACCI NUMBERS

In mathematics, the Fibonacci numbers or Fibonacci series or Fibonacci sequence are the numbers in the following integer sequence:

$$
0,1,1,2,3,5,8,13,21,34,55,89,144, \ldots
$$

By definition, the first two numbers in the Fibonacci sequence are 0 and 1 , and each subsequent number is the sum of the previous two. In mathematical terms, the sequence $F_{n}$ of Fibonacci numbers is defined by the recurrence relation

$$
\begin{equation*}
F_{n}=F_{n-1}+F_{n-2}, \tag{3.1}
\end{equation*}
$$

with seed values

$$
\begin{equation*}
F_{0}=0, F_{1}=1 . \tag{3.2}
\end{equation*}
$$

The Fibonacci sequence is named after Leonardo Fibonacci. His 1202 book Liber Abaci introduced the sequence to Western European mathematics, although the sequence had been described earlier in Indian mathematics. Goonatilake (1998) By modern convention, the sequence begins either with $F_{0}=0$ or with $F_{1}=1$. The Liber Abaci began the sequence with $F_{1}=1$, without an initial 0.

### 3.1 Origins

The Fibonacci sequence appears in Indian mathematics, in connection with Sanskrit prosody. Singh (1985) In the Sanskrit oral tradition, there was much emphasis on how long (L) syllables mix with the short (S), and counting the different patterns of L and S within a given fixed length results in the Fibonacci numbers; the number of patterns that are m short syllables long is the Fibonacci number $F_{m+1}$. Goonatilake (1998) writes that the development of the Fibonacci sequence "is attributed in part to Pingala ( 200 BC ), later being associated with Virahanka (c. 700 AD), Gopala (c. 1135), and Hemachandra (c. 1150)".

### 3.2 List of Fibonacci Numbers

The first 11 Fibonacci numbers $F_{n}$ for $n=0,1,2, \ldots, 10$ are:
The sequence can also be extended to negative index $n$ using the re-arranged recurrence relation

$$
\begin{equation*}
F_{n-2}=F_{n}-F_{n-1}, \tag{3.3}
\end{equation*}
$$

which yields the sequence of "negafibonacci" numbers satisfying

$$
\begin{equation*}
F_{-n}=(-1)^{n+1} F_{n} . \tag{3.4}
\end{equation*}
$$

Thus the bidirectional sequence is
Rohl (1989) gives an account of how Fibonacci numbers can be computed efficiently.


Figure 3.1: A page of Fibonacci's Liber Abaci a very long title e just to prove my point more and more and more
Source: Heinz Lüneburg, Leonardi Pisani Liber Abaci oder Lesevergnügen eines
Mathematikers

Table 3.1: First 11 Fibonacci Numbers for $n=0,1, \ldots$

| $F_{0}$ | $F_{1}$ | $F_{2}$ | $F_{3}$ | $F_{4}$ | $F_{5}$ | $F_{6}$ | $F_{7}$ | $F_{8}$ | $F_{9}$ | $F_{10}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 0 | 1 | 1 | 2 | 3 | 5 | 8 | 13 | 21 | 34 | 55 |

Table 3.2: Bidirectional Fibonacci Numbers sequence

| $F_{-5}$ | $F_{-4}$ | $F_{-3}$ | $F_{-2}$ | $F_{-1}$ | $F_{0}$ | $F_{1}$ | $F_{2}$ | $F_{3}$ | $F_{4}$ | $F_{5}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 5 | -3 | 2 | -1 | 1 | 0 | 1 | 1 | 2 | 3 | 5 |

### 3.3 Applications

### 3.3.1 In Computation

Fibonacci numbers have wide applications in mathematics as well as computer science:

- The Fibonacci numbers are important in the computational run-time analysis of Euclid's algorithm to determine the greatest common divisor of two integers: the worst case input for this algorithm is a pair of consecutive Fibonacci numbers.
- Yuri Matiyasevich was able to show that the Fibonacci numbers can be defined by a Diophantine equation, which led to his original solution of Hilbert's tenth problem.
- The Fibonacci numbers are also an example of a complete sequence. This means that every positive integer can be written as a sum of Fibonacci numbers, where any one number is used once at most.
- Moreover, every positive integer can be written in a unique way as the sum of one or more distinct Fibonacci numbers in such a way that the sum does not include any two consecutive Fibonacci numbers. This is known as Zeckendorf's theorem, and a sum of Fibonacci numbers that satisfies these conditions is called a Zeckendorf representation. The Zeckendorf representation of a number can be used to derive its Fibonacci coding.
- Fibonacci numbers are used by some pseudorandom number generators.
- Fibonacci numbers are used in a polyphase version of the merge sort algorithm in which an unsorted list is divided into two lists whose lengths correspond to sequential Fibonacci numbers - by dividing the list so that the two parts have lengths in the approximate proportion $\varphi$. A tape-drive implementation of the polyphase merge sort was described in The Art of Computer Programming.
- Fibonacci numbers arise in the analysis of the Fibonacci heap data structure.
- The Fibonacci cube is an undirected graph with a Fibonacci number of nodes that has been proposed as a network topology for parallel computing.
- A one-dimensional optimization method, called the Fibonacci search technique, uses Fibonacci numbers.
- The Fibonacci number series is used for optional lossy compression in the IFF 8SVX audio file format used on Amiga computers. The number series compands the original audio wave similar to logarithmic methods such as $\mu$-law.
- Since the conversion factor 1.609344 for miles to kilometers is close to the golden ratio (denoted $\varphi$ ), the decomposition of distance in miles into a sum of Fibonacci numbers becomes nearly the kilometer sum when the Fibonacci numbers are replaced by their successors. This method amounts to a radix 2 number register in golden ratio base $\varphi$ being shifted. To convert from kilometers to miles, shift the register down the Fibonacci sequence instead.


### 3.3.2 In Nature

Fibonacci sequences appear in biological settings, in two consecutive Fibonacci numbers, such as branching in trees, arrangement of leaves on a stem, the fruitlets of a pineapple, the flowering of artichoke, an uncurling fern and the arrangement of a pine cone, and the family tree of honeybees. However, numerous poorly substantiated claims of Fibonacci numbers or golden sections in nature are found in popular sources, e.g., relating to the breeding of rabbits in Fibonacci's own unrealistic example, the seeds on a sunflower, the spirals of shells, and the curve of waves.

A model for the pattern of florets in the head of a sunflower was proposed by H. Vogel in 1979. Vogel (1979) This has the form

$$
\begin{equation*}
\theta=\frac{2 \pi}{\phi^{2}} n, r=c \sqrt{n} \tag{3.5}
\end{equation*}
$$

where $n$ is the index number of the floret and $c$ is a constant scaling factor; the florets thus lie on Fermat's spiral.


Figure 3.2: Yellow Chamomile head

## CHAPTER 4

## GOLDEN RATIO

In mathematics and the arts, two quantities are in the golden ratio if their ratio is the same as the ratio of their sum to the larger of the two quantities, i.e. their maximum. The figure on the right illustrates the geometric relationship. Expressed algebraically, for quantities $a$ and $b$ with $a>b$,

$$
\begin{equation*}
\frac{a+b}{a}=\frac{a}{b} \stackrel{\text { def }}{=} \varphi, \tag{4.1}
\end{equation*}
$$

where the Greek letter $\varphi$ represents the golden ratio. Its value is:

$$
\begin{equation*}
\varphi=\frac{1+\sqrt{5}}{2}=1.6180339887 \ldots \tag{4.2}
\end{equation*}
$$

### 4.1 History

Ancient Greek mathematicians first studied what we now call the golden ratio because of its frequent appearance in geometry. The division of a line into "extreme and mean ratio" (the golden section) is important in the geometry of regular pentagrams and pentagons. Euclid's Elements provides the first known written definition of what is now called the golden ratio: "A straight line is said to have been cut in extreme and mean ratio when, as the whole line is to the greater segment, so is the greater to the less." Euclid explains a construction for cutting (sectioning) a line "in extreme and mean ratio", i.e., the golden ratio. (See Figure 4.1.) Throughout the Elements, several propositions (theorems in modern terminology) and their proofs employ the golden ratio.

### 4.2 Calculation

Two quantities $a$ and $b$ are said to be in the golden ratio $\varphi$ if:

$$
\begin{equation*}
\frac{a+b}{a}=\frac{a}{b}=\varphi . \tag{4.3}
\end{equation*}
$$

One method for finding the value of $\varphi$ is to start with the left fraction. Through simplifying the fraction and substituting in $\frac{b}{a}=\frac{1}{\varphi}$,

$$
\begin{equation*}
\frac{a+b}{a}=1+\frac{b}{a}=1+\frac{1}{\varphi} \tag{4.4}
\end{equation*}
$$

By definition, it is shown that

$$
\begin{equation*}
1+\frac{1}{\varphi}=\varphi \tag{4.5}
\end{equation*}
$$

Multiplying by $\varphi$ gives

$$
\varphi+1=\varphi^{2}
$$

which can be rearranged to

$$
\varphi^{2}-\varphi-1=0 .
$$

Using the quadratic formula, two solutions are obtained:

$$
\varphi=\frac{1+\sqrt{5}}{2}=1.6180339887 \ldots
$$

and

$$
\varphi=\frac{1-\sqrt{5}}{2}=-0.6180339887 \ldots
$$

Because $\varphi$ is the ratio between positive quantities $\varphi$ is necessarily positive:

$$
\varphi=\frac{1+\sqrt{5}}{2}=1.6180339887 \ldots
$$

Different representations of the golden ratio are given in Table 4.1.

$a+b$ is to $a$ as $a$ is to $b$
Figure 4.1: Line segments in the golden ratio


Figure 4.2: Golden rectangles

Table 4.1: Number representations of the golden ratio

| Form | Representation |
| :--- | :--- |
| Binary | $1.100111000110111011 \ldots$ |
| Decimal | $1.6180339887498948482 \ldots$ |
| Hexadecimal | $1.9 \mathrm{E} 3779 \mathrm{~B} 97 \mathrm{~F} 4 \mathrm{~A} 7 \mathrm{C} 15 \mathrm{~F} 39 \ldots$ |
| Continued fraction | $1+\frac{1}{1+\frac{1}{1+\frac{1}{1+\frac{1}{1+\ddots}}}}$ |
| Algebraic form | $\frac{1+\sqrt{5}}{2}$ |
| Infinite series | $\frac{13}{8}+\sum_{n=0}^{\infty} \frac{(-1)^{(n+1)}(2 n+1)!}{(n+2)!n!4^{(2 n+3)}}$ |

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## APPENDIX A

## DETAILS

Lorem ipsum dolor sit amet, consectetur adipiscing elit. Donec posuere, neque quis feugiat egestas, quam sapien dictum justo, eu vulputate nunc metus sed dui. Integer molestie leo quis libero facilisis, dictum pretium quam ornare. Vestibulum ante ipsum primis in faucibus orci luctus et ultrices posuere cubilia Curae; Vivamus luctus rutrum magna non convallis. Praesent vestibulum consequat eros, et fringilla nisi suscipit id. Nam vulputate justo dui, eu rutrum est accumsan ut. Sed molestie erat vitae mi blandit, in volutpat urna lobortis. Vestibulum mollis rutrum gravida. Fusce dolor nulla, condimentum vel pretium ut, venenatis eget leo. Ut semper placerat mauris, ut tempus est tempor vel. Interdum et malesuada fames ac ante ipsum primis in faucibus. In vitae feugiat diam. Pellentesque accumsan consequat turpis aliquam elementum.

## APPENDIX B

## SOFTWARE CODE

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