

# Spectral Delay Filters\*

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This paper discusses the implementation of spectral delay using filters comprising a cascade of many low-order allpass filters and an equalizing filter. The spectral delay filters have chirp-like impulse responses causing a large, frequency-dependent delay that is useful in audio effects processing. An equalizing filter design and a multirate technique, which stretches the allpass filters, impulse response, are introduced.

## 0 INTRODUCTION

Filtering an audio signal with an allpass filter does not usually have a major effect on the signal's timbre. The allpass filter does not change the frequency content of the signal, but only introduces a phase shift or delay. Audibility of the phase distortion caused by an allpass filter in a sound reproduction system has been a topic of many studies, see, e.g., [1], [2]. In this paper, we investigate audio effects processing using high-order allpass filters that consist of many cascaded low-order allpass filters. These filters have long chirp-like impulse responses. When audio and music signals are processed with such a filter, remarkable changes are obtained that are similar to the spectral delay effect [3], [4].

## 1 CHIRP-LIKE IMPULSE RESPONSES AND GROUP DELAY

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$$A(z) = \frac{a_1 + z^{-1}}{1 + a_1 z^{-1}}, \quad (1)$$

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$$\tau_{g,\max} = \begin{cases} \tau_g(0) = \frac{1-a_1}{1+a_1}, & \text{when } a_1 \leq 0 \\ \tau_g(\pi) = \frac{1+a_1}{1-a_1}, & \text{when } a_1 > 0. \end{cases} \quad (2)$$

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- 1) Green-function determined experimentally and published.
- 2) Black-function determined using similarity searches and published.
- 3) Red-function determined using similarity searches and determined in this study.
- 4) Blue-O-antigen structure unknown. Function determined using similarity searches and proposed in this study.

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Table 1. Active sites and allosteric sites of the GNE MNK enzyme

Excerpt No.	Genre	Spatial Mode	Correlation
1	Pop	FB	94%
2	Classical	FB	33%
3	Jazz	FF	76%
4	Arabian	FF	41%
5	GNE	H220	45%
6	GNE	H45	93%
7	MNK	G416	74%
8	MNK	D413	72%
9	MNK	R420	94%
10	MNK	N516	91%

Note. This table does not include sentence enhancement statuses. This table does not include sentence enhancement statuses.

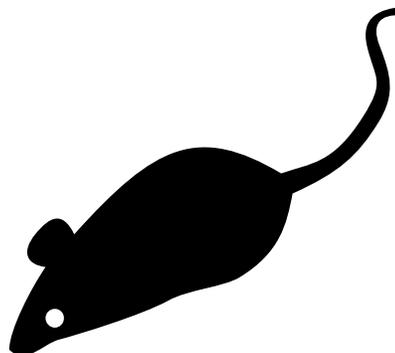


Fig. 1. The spectral delay filter consists of  $M$  allpass filters and an equalization filter.

<sup>1</sup>This point is emphasized by Loewer, see esp. p. (610).

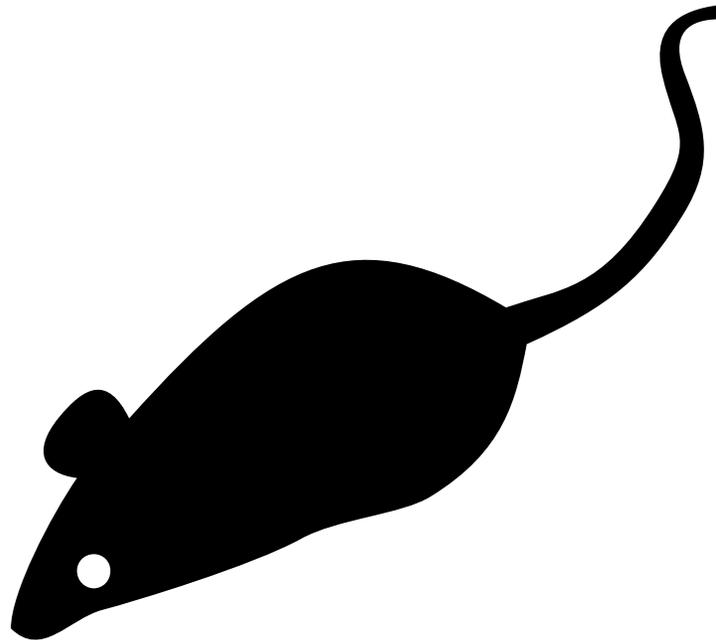


Fig. 2. This paper is organized as follows. In Section 1, we discuss the group delay of a cascade of first-order allpass filters and its relation to the chirp-like impulse response of the spectral delay filter. Furthermore, a multirate method to stretch the impulse response of the spectral delay filter is proposed. Section 2 discusses the amplitude envelope of the impulse response and suggests a design method for the equalizing filter. Section 3 presents application examples using the spectral delay filter. Section 4 concludes this paper.

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$$\tau_g(\omega) = -\frac{d\phi(\omega)}{d\omega}.$$

Audibility of the phase distortion caused by an allpass filter in a sound reproduction system has been a topic of many studies, see, e.g., [1], [2]. In this paper, we investigate audio effects processing using high-order allpass filters that consist of many cascaded low-order allpass filters. These filters have long chirp-like impulse responses. When audio and music signals are processed with such a filter, remarkable changes are obtained that are similar to the spectral delay effect.

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## 2 SUMMARY

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## 3 CONCLUSION

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## 4 ACKNOWLEDGMENT

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## APPENDIX

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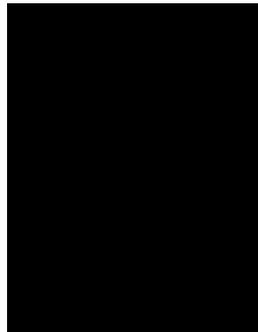
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**NOMENCLATURE**

$a_c$  = condensation coefficient condensation coefficient condensation coefficient

TLR = Toll-like receptor

PAMPs = pathogen-associated molecular patterns condensation coefficient condensation

**THE AUTHORS**

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